



**A polarized adding-doubling
radiative transfer model
for simulating multi-layer scattering atmospheres**

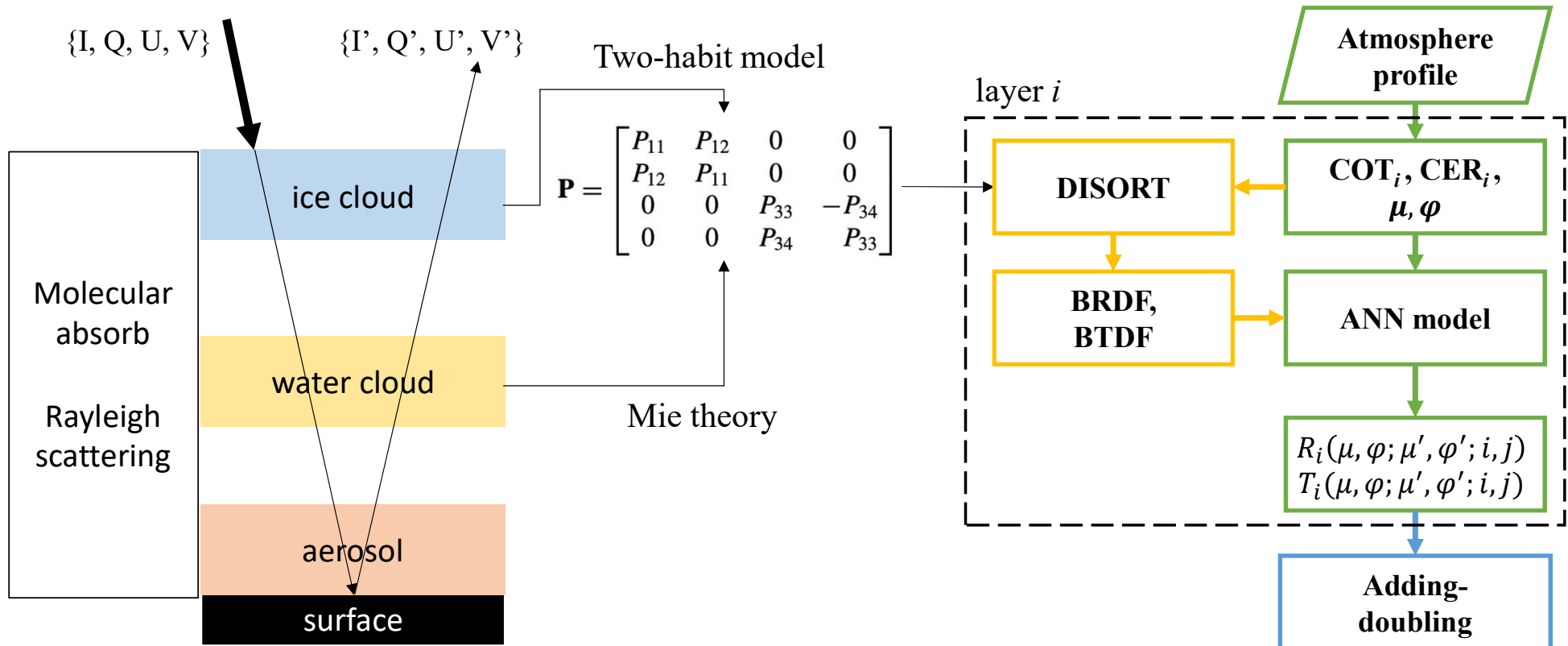
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1 Background

- RTMs that solve multi-layered atmosphere
 - RRTM(G/GP) (Lagerquist et al., 2021; Liu et al., 2020; Ukkonen, 2022)
 - libRadtran (Taylor et al., 2016; Brence et al., 2022)
 - Adding-Doubling method (Van de Haulst, 1980; Huang et al., 2015)
- Current NNs are trained to emulate RTMs
 - trained separately for clear/cloudy skies
 - not universal for multilayer clouds (~12% occurrence, Yuan and Oreopoulos, 2013)
 - not applicable for polarized light

2 Method

Multi-layer scattering atmosphere



2 Method

ANN model

Layer	Shape	Activation
Input	6	None
Dense 1	256	LeakyRelu
Dense 2	128	LeakyRelu
Dense 3	64	LeakyRelu
Output	16	None

Activation: LeakyRelu

$$y = \begin{cases} 0.2x, & \text{if } x \leq 0 \\ x, & \text{if } x > 0 \end{cases}$$

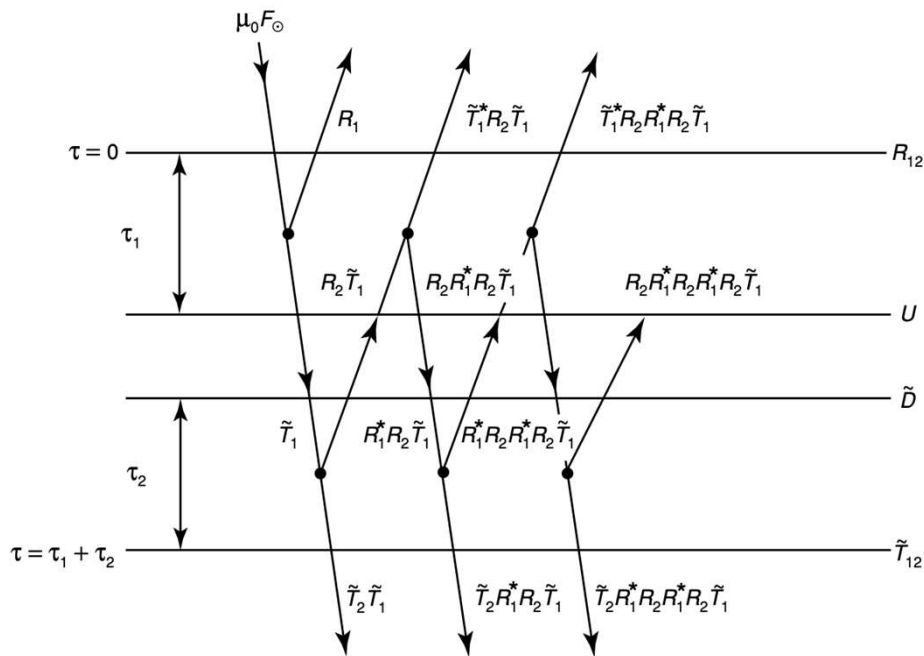
loss: Huber

$$L_{\delta}(y, f(x)) = \begin{cases} \frac{1}{2}(y - f(x))^2, & \text{if } |y - f(x)| \leq \delta \\ \delta|y - f(x)| - \frac{1}{2}\delta^2, & \text{if } |y - f(x)| > \delta \end{cases}$$

$$\delta = 1$$

2 Method

Adding-doubling method



(Liou, 2002)

$$\begin{aligned}\tilde{D} &= \tilde{T}_1 + R_1^* R_2 \tilde{T}_1 + R_1^* R_2 R_1^* R_2 \tilde{T}_1 + \dots \\ &= \left[1 + R_1^* R_2 + (R_1^* R_2)^2 + \dots \right] \tilde{T}_1 \\ &= (1 - R_1^* R_2)^{-1} \tilde{T}_1\end{aligned}$$

$$U = R_2 \tilde{D}$$

$$R_{12} = R_1 + \tilde{T}_1^* U$$

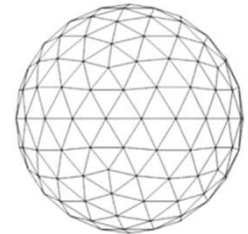
$$\tilde{T}_{12} = \tilde{T}_2 \tilde{D}$$

$$R_1^* R_2 = \frac{1}{\pi} \int_0^{2\pi} \int_0^1 R_1^*(\mu, \phi, \mu', \phi') R_2(\mu', \phi', \mu_0, \phi_0) \mu' d\mu' d\phi'$$

$$X(\mu, \phi) * Y(\mu, \phi) = f \sum_{i=1}^N X_i Y_i \mu_i A_i,$$

$$f = \frac{2}{\sum_{i=1}^N A_i} = \frac{2}{5}.$$

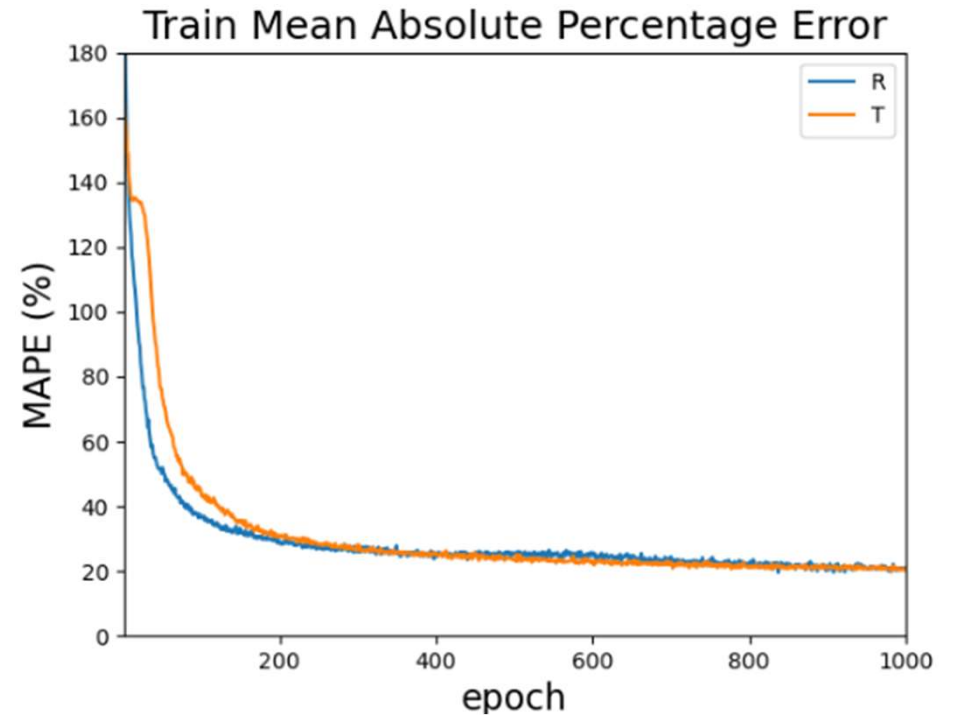
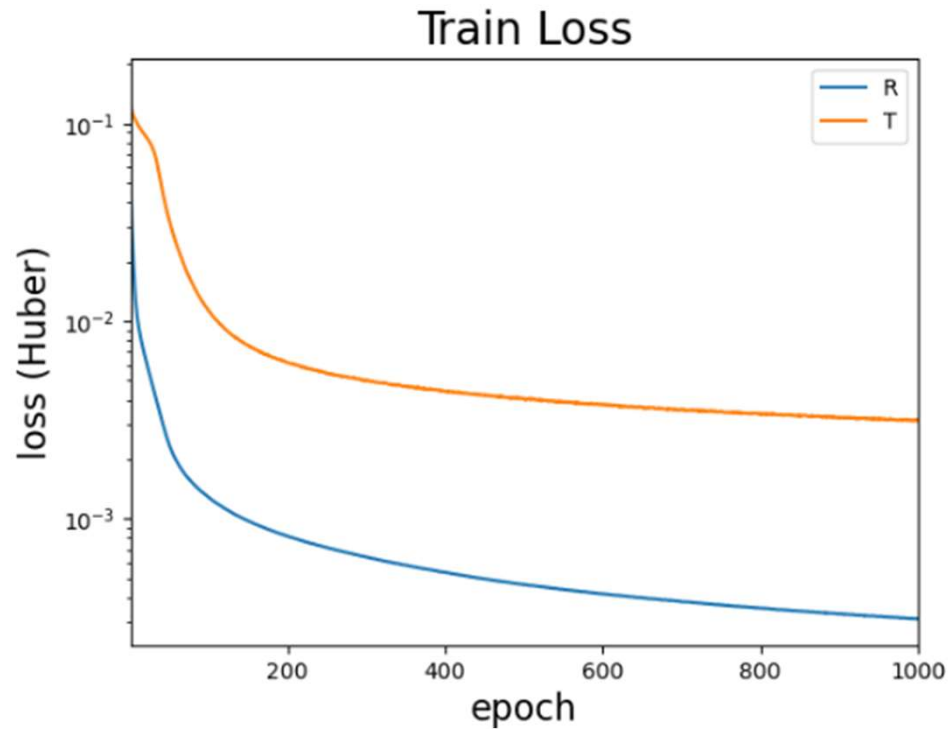
N=320



(Wang et al., 2013)

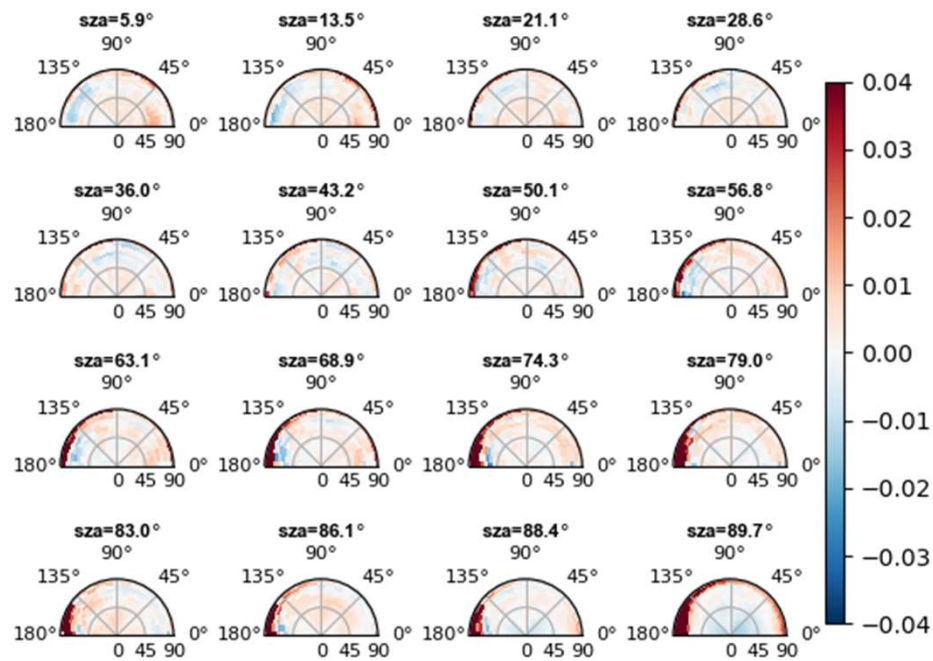
3 Results

ANN training



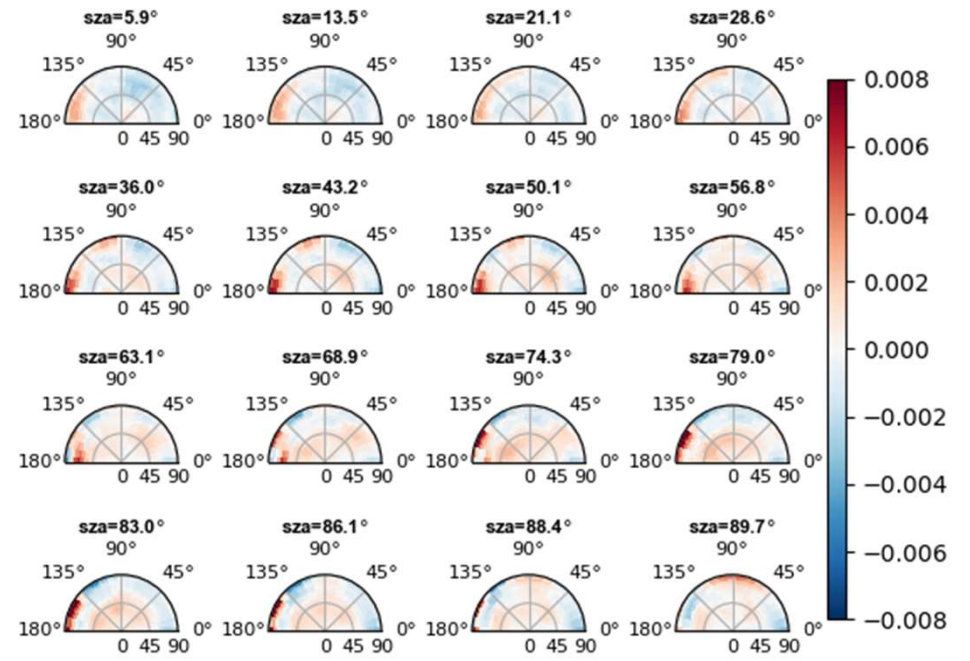
3 Results

Single layer accuracy



Bias of R11

Ice cloud
wavelength = $0.8\mu\text{m}$
COT=1; CER=10

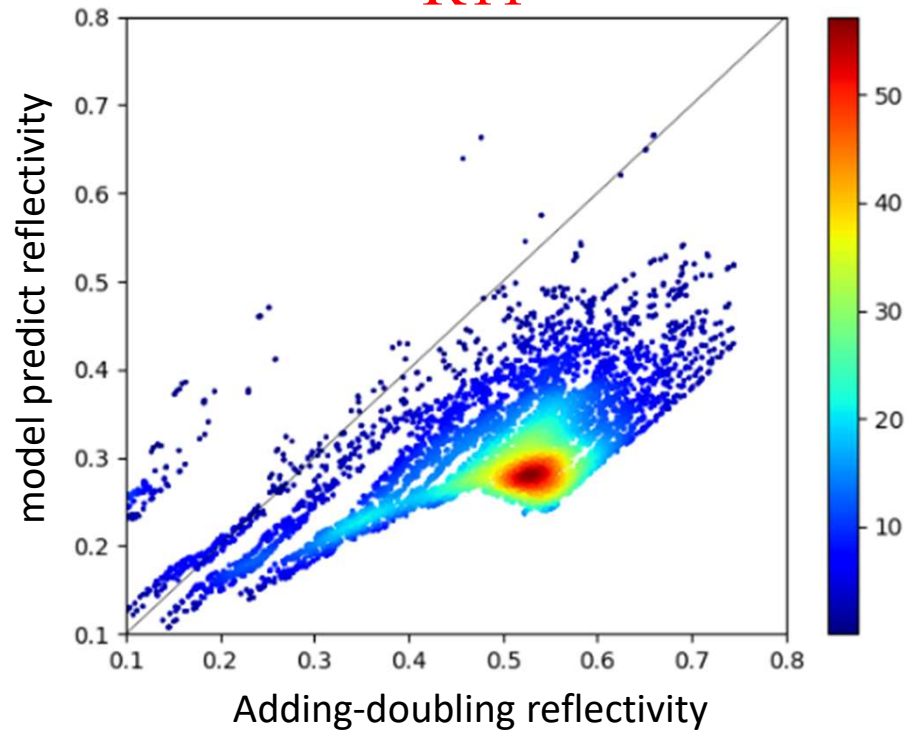


Bias of R12

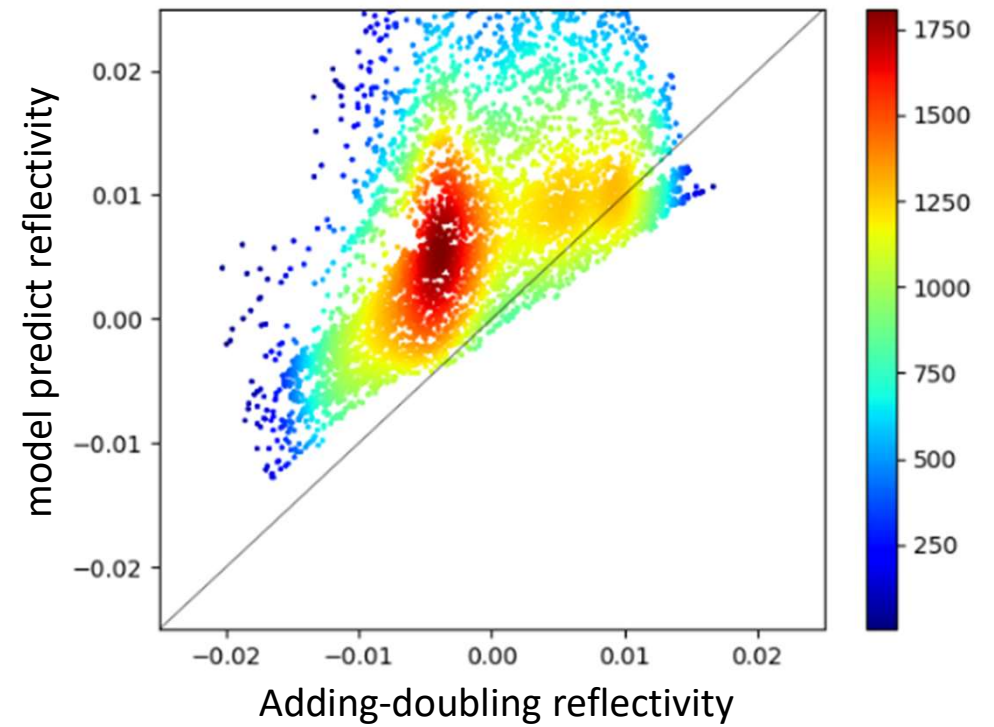
3 Results

Combination of two given layers

R11



R12



Polarized adding-doubling RTM

➤ Acceleration:

from 7,000s to 7s when calculating BRDF of two-layer cloud
between 320 incidence angles (10^3 times speed up)

➤ Accuracy:

ANN achieved an MAPE of 20% for ice cloud layer

$R = 0.67$ for BRDF of two-layer cloud

Problems to be solved

- Underestimate of former scattering
- Improve the accuracy of adding procedure
- Asymmetry effect of polarized light



Thank You!